



Mathematical Optimization of Process Flowsheet with Water Integration



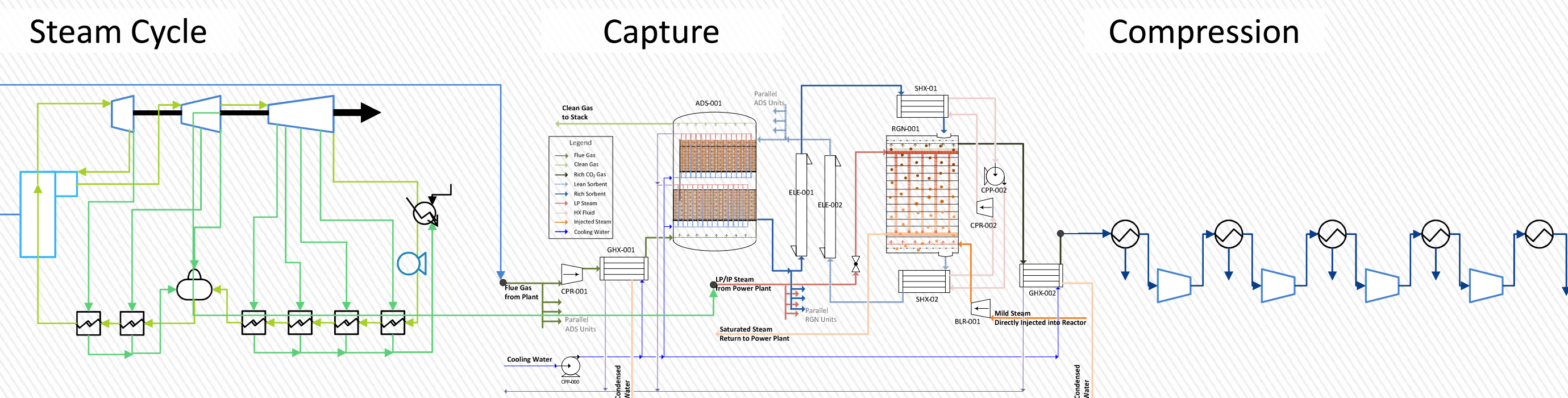
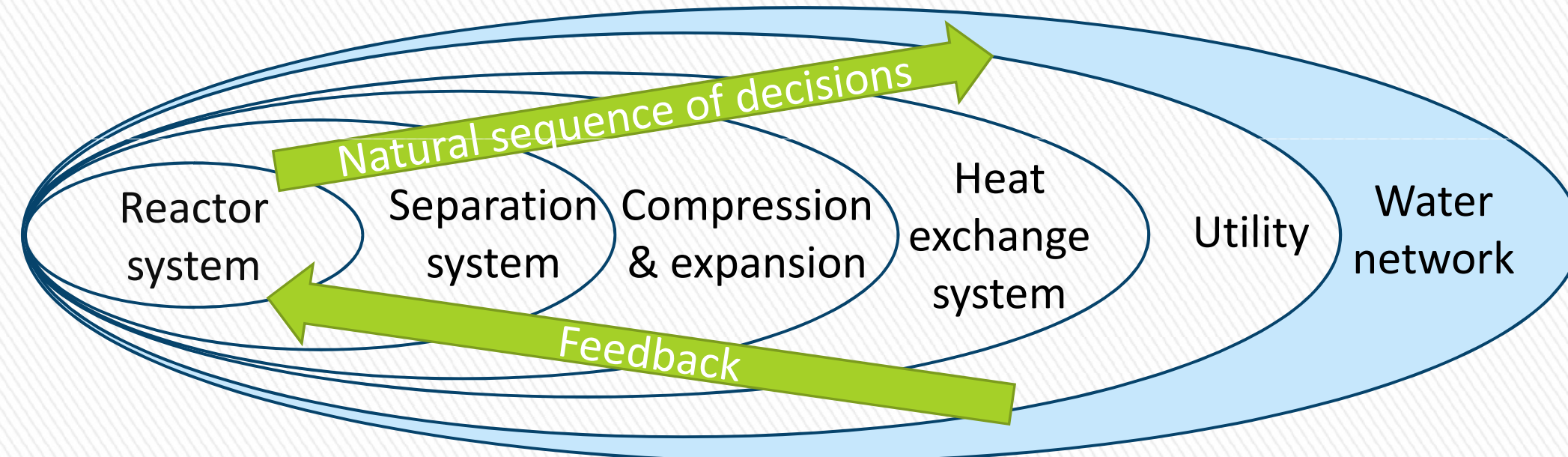
- PC Plant with CO₂ Capture

Linlin Yang and Ignacio E. Grossmann

Department of Chemical Engineering, Carnegie Mellon University, Pittsburgh, PA 15213

Motivation for Simultaneous Optimization

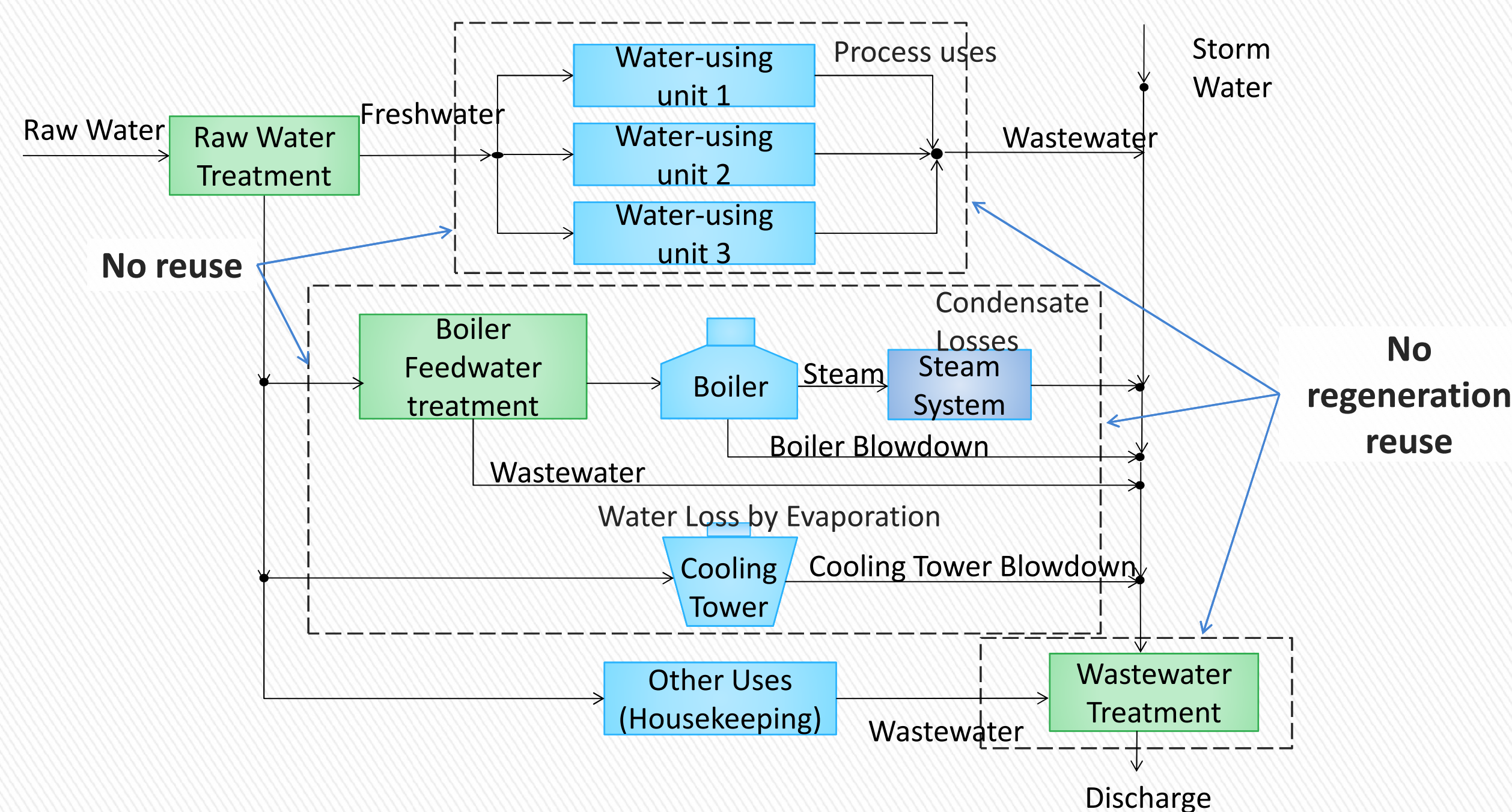
- In process synthesis, subsystems are designed after process flowsheet in a sequential fashion^[5]
- Simultaneous optimization** can capture tradeoffs among raw material, investment cost and operating cost
- Interest of this work to develop a method to perform simultaneous optimization to account for the feedbacks to the flowsheet from heat integration and **water integration**, and apply the method to **CO₂ capture utility allocation problem**



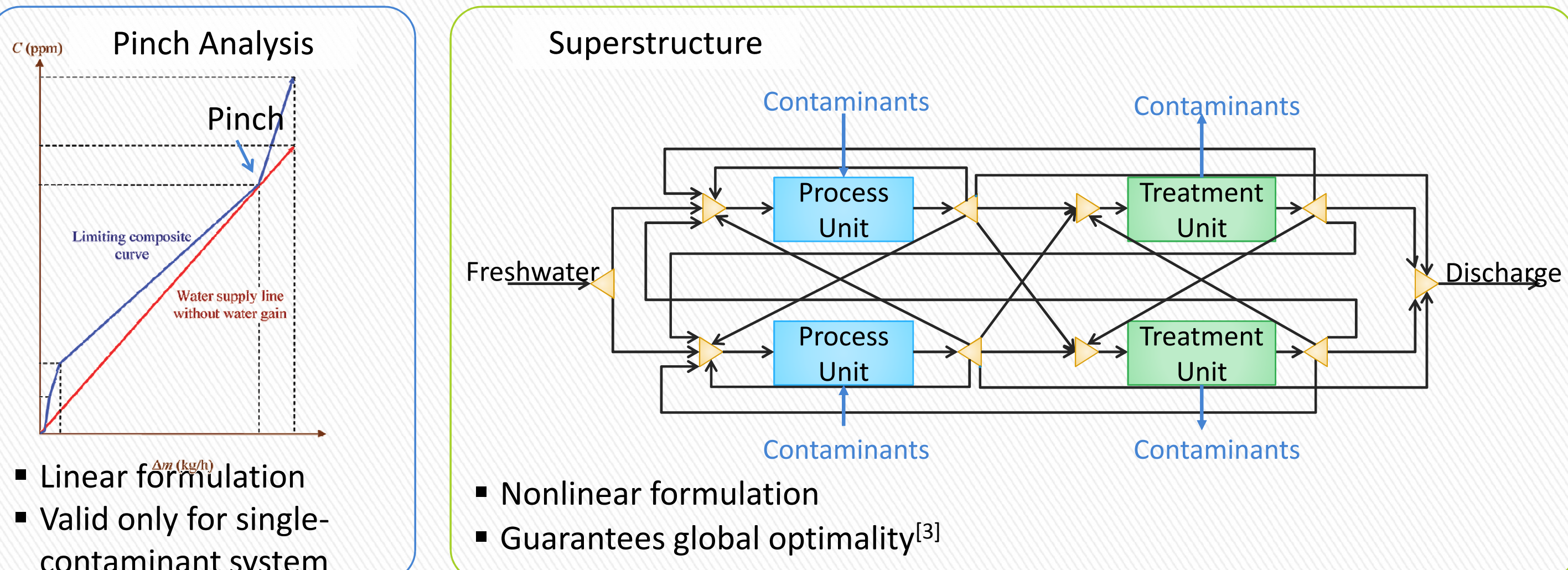
- Boiler feedwater**
- Electricity required for FW pump
- Turbine generates electricity and steam
- Requires cooling water in the condenser
- Requires steam in the regenerator
- Requires cooling water
- Requires cooling water for isothermal compression
- Requires electricity for compression
- Generates wastewater from condensation

Water Network Synthesis Methods

Conventional water network in the process industry does not allow for reuse of water streams



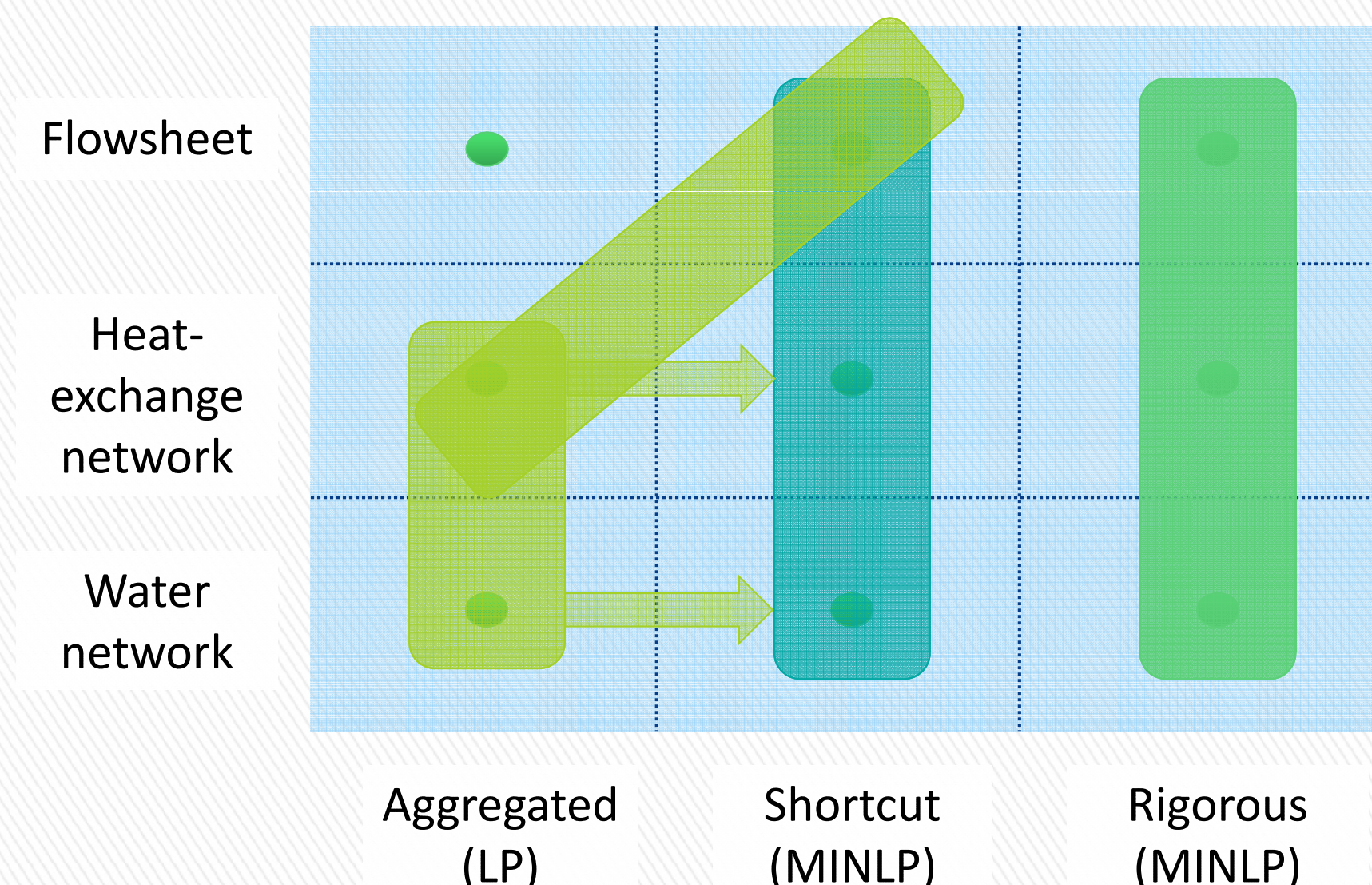
There are two general approaches to perform water network synthesis, this work uses the superstructure-based approach for water integration



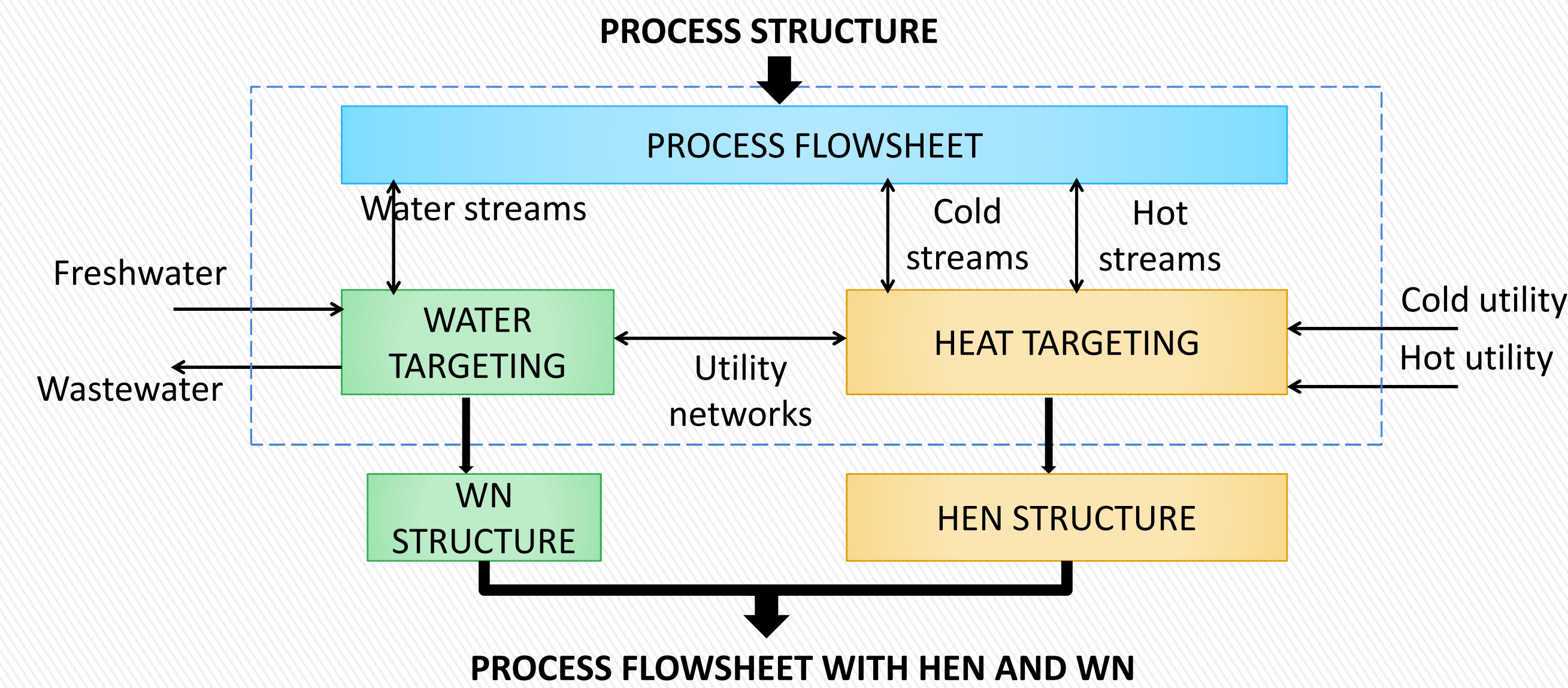
Simultaneous Process Flowsheet / HEN / WN Integration

Targeting approach is used to **evaluate system performance** without commitment to detailed design. It is used to avoid solving a large nonconvex MINLP network models

- Path 0: Unrealistic to solve (large MINLP)
- Path 1: Very difficult to solve (MINLP)
- Path 2: Can we avoid solving that MINLP but still get to the same optimal solution?



The strategy is to first optimize flowsheet operating conditions and the target requirement, then in the subsequent step determine the WN and HEN structures



$$\min. \phi = F(x, u, v) + \sum_{i \in HU} c_H^i Q_H^i + \sum_{j \in CU} c_C^j Q_C^j + c_{fw} F_{fw}$$

$$\text{s.t. } h^P(x, u, v) = 0$$

$$g^P(x, u, v) \leq 0$$

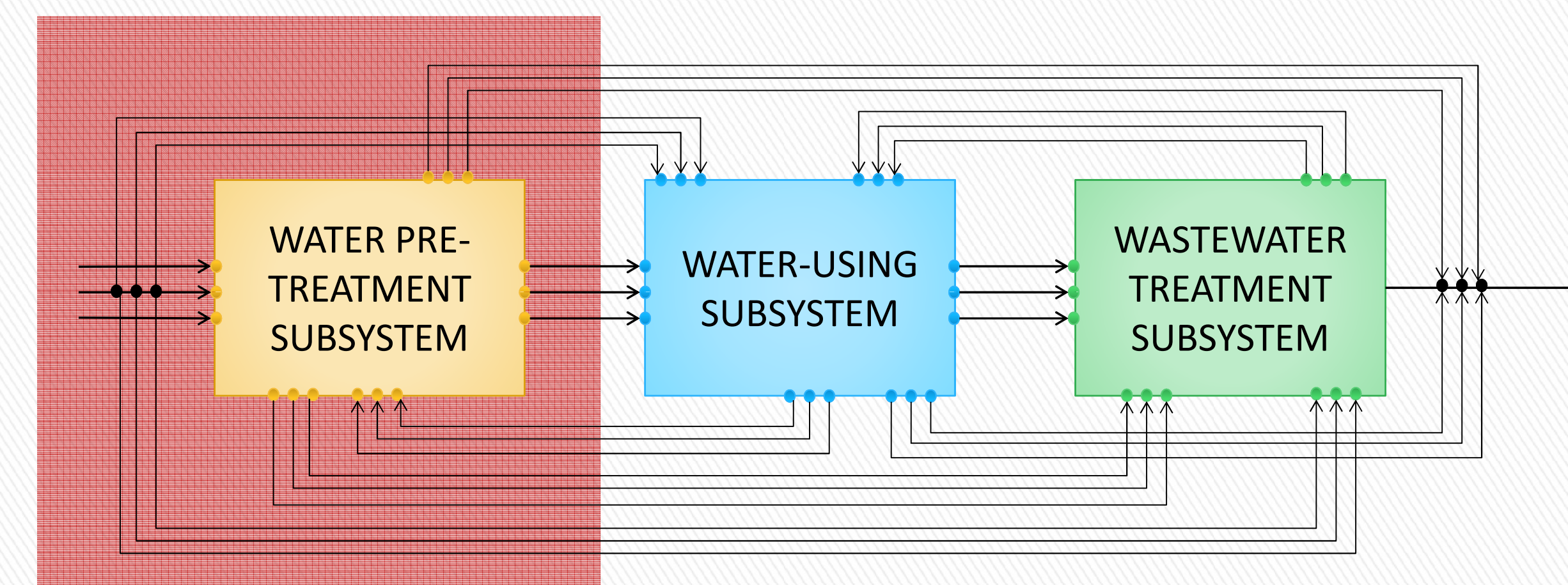
$$g^{HEN}(u, Q_H, Q_C) \leq 0$$

$$g^{WN}(v, F_{fw}) \leq 0 \quad \text{Need to derive this targeting formulation}$$

$$x \in X, \quad u \in U, \quad v \in V$$

Rethinking Water Network Architecture

- We cannot take it for granted that freshwater is of high purity
- Need to design the **proper architecture** of water network^[1] such that it contains pretreatment processes to generate freshwater of **high purity** (e.g. to satisfy demands in boilers)



Water Targeting Method for Process Use

We have developed a water targeting formulation that relaxes the **nonlinear** water network formulation into **linear** formulation. The proposed LP model predicts the **exact** target for minimum freshwater consumption of a set of water-using processes under some assumptions.

$$F^k = \sum_{m \in MU, k \in m_{out}} F^i \quad \forall m \in MU, k \in m_{out}$$

$$F_i C_i^k = \sum_{m \in MU, k \in m_{out}} F_j C_j^k \quad \forall j, \forall m \in MU, k \in m_{out}$$

Bilinear terms

$$F^k = \sum_{s \in SU, k \in s_m} F^i \quad \forall s \in SU, k \in s_m$$

$$C_j^k = C_j^i \quad \forall j, \forall s \in SU, \forall i \in s_{out}, k \in s_m$$

$$P_m^i C_i^k + L_j = r_{out} C_j^k \quad \forall j, \forall p \in PU, k \in p_{in}, i \in p_{out}$$

$$C_j^k \leq C_j^i \leq C_j^{k,max} \quad \forall j, k$$

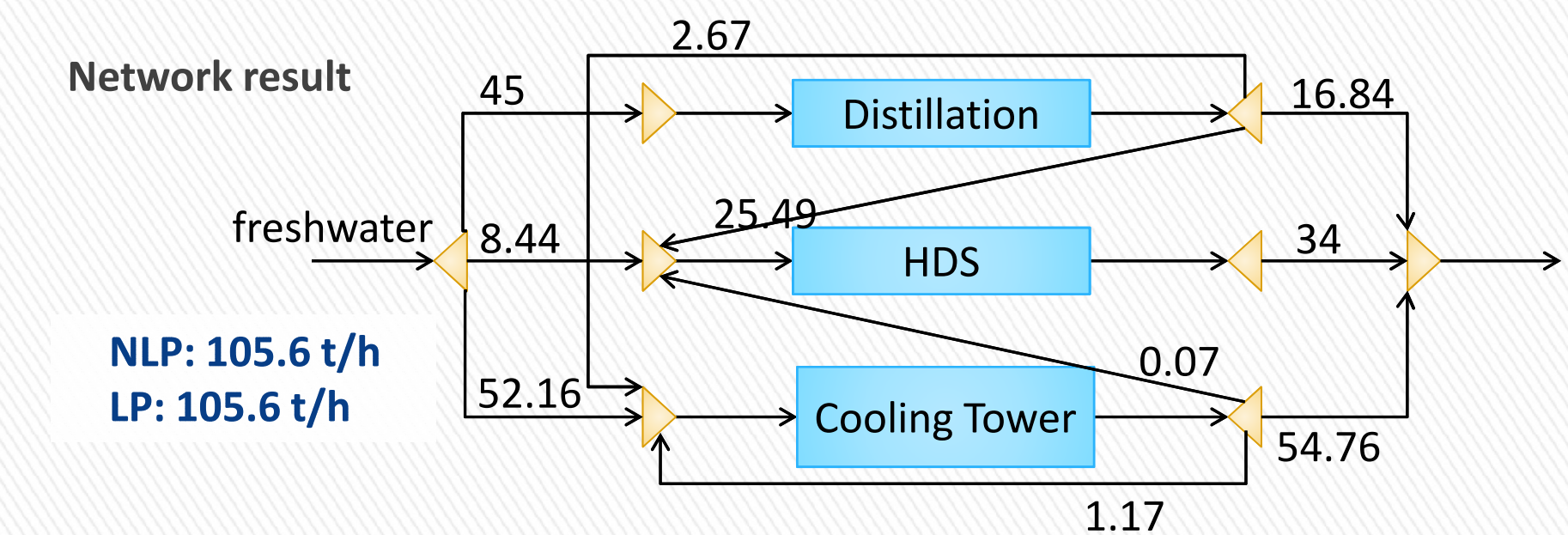
Process Unit

$$F^k = F^i \quad \forall i \in TU, \forall i \in t_{out}, \forall k \in t_{in}$$

$$C_j^k = \beta_j C_j^i \quad \forall j, \forall i \in TU, \forall i \in t_{out}, \forall k \in t_{in}$$

Treatment Unit

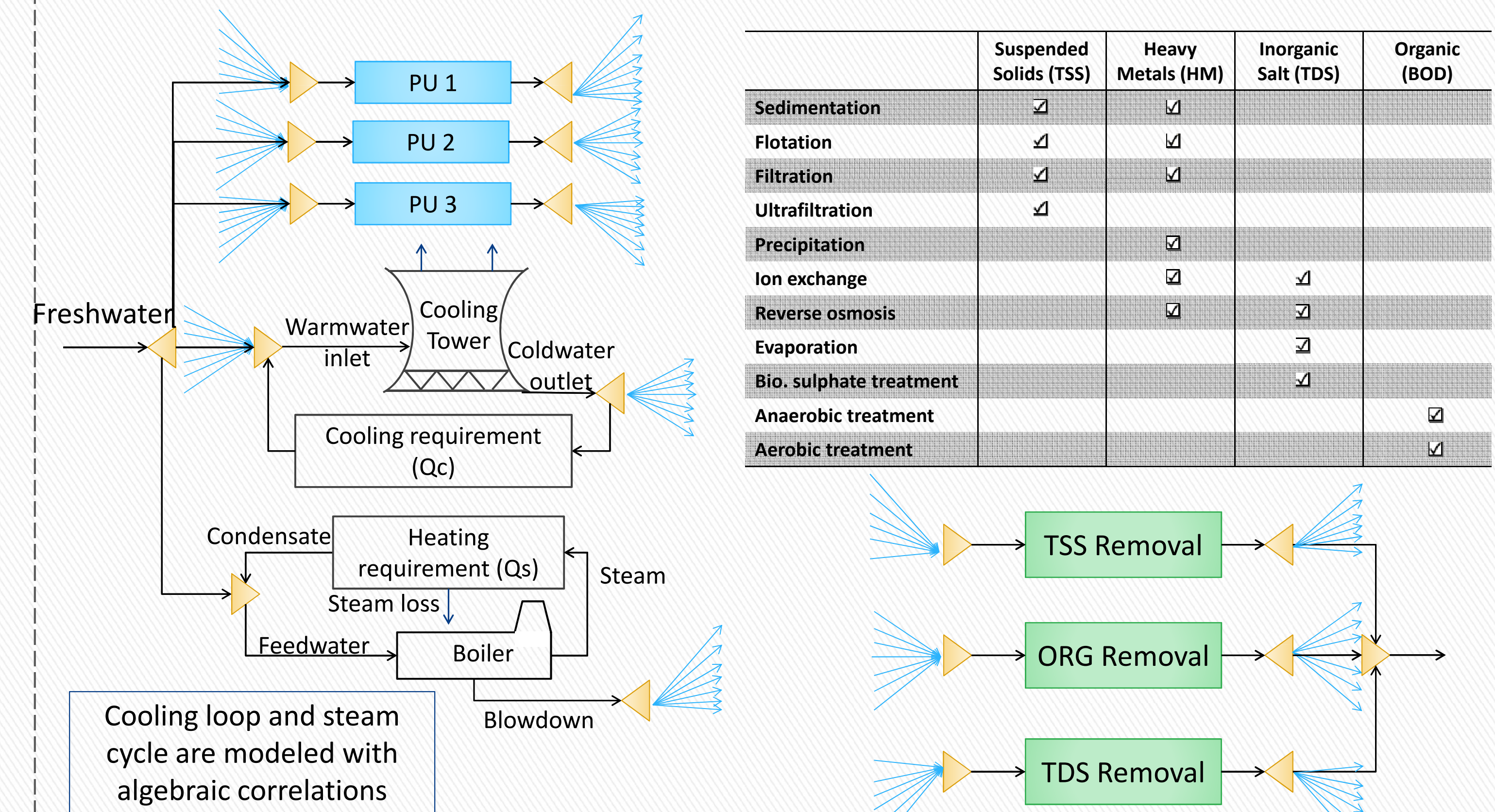
	Distillation			HDS			Cooling Tower		
	C _{j,x} ^{pin,max} (ppm)	Load (kg/h)	F (ton/h)	C _{j,x} ^{pin,max} (ppm)	Load (kg/h)	F (ton/h)	C _{j,max} ^{pin} (ppm)	Load (kg/h)	F (ton/h)
HC	0	0.675		20	3.4		120	5.6	
H ₂ S	0	18	45	300	414.8	34	20	1.4	56
Salt	0	1.575		45	4.59		200	520.8	



Using the targeting approach, the freshwater consumption is 105.6 ton/hr, which is a significant saving over 135 ton/hr required for conventional water network

Considerations for Process Units & Treatment Units

The goal is to select a subset of BAT technologies^[6] and flowrates that best fit the treatment of the receiving wastewater streams



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