# Non-intrusive UQ Methods and Software for Engineering Applications

SIAM UQ Conference April 3, 2012

#### Lawrence Livermore National Laboratory

### Charles Tong



LLNL-PRES-XXXXXX

This work was performed under the auspices of the U.S. Department of Energy by Lawrence Livermore National Laboratory under contract DE-AC52-07NA27344. Lawrence Livermore National Security, LLC

### Outline

- A few applications
- A UQ Process
- Methods for propagation and analysis of uncertainties
- A UQ software: PSUADE
- Usage examples



## **Carbon Capture Simulation Initiative**



Goal is to develop M&S tools to accelerate the commercialization of Carbon Capture Technologies

# Assess different CC technology via simulation and modeling



Lawrence Livermore National Laboratory

LLNL-PRES-XXXXXX

# Can we use the world's most abundant and widely distributed fossil fuel source in a different way?



An artist's rendition depicts the goal of the FutureGen initiative, which aims to build the world's first integrated sequestration and hydrogen production research power plant based on coal gasification.

Source: DOE Office of Fossil Energy

As part of Clean Coal Initiative developing advanced coal technologies based on **GASIFICATION** to achieve zero emission of pollutants (CO2) while still remaining economically competitive

Source: Aytekin Gel's various presentations



Source: Overview of Gasification Technologies, Gary J. Stiegel, NETL (2005)



## Challenge: How can we design commercial scale gasifiers for optimized operation?





# **NRAP: UQ of Geochemical Impact of CO<sub>2</sub> Leakage into Aquifers**



- 3D Heterogeneous domain of 10000× 10000×240 to represent High Plains aquifer including saturated and unsaturated zones
- Two geologic facies: sand and clay
- Regional groundwater flow is maintained by 0.3% hydraulic gradient
- A single leakage source is at (4500.0, 0.0, 198.41)
- Time steps = 103 for 100 years

Structure Model	NUFT Model	
<ul> <li>Sand volume fraction</li> <li>Correlation length in x</li> <li>Correlation length in y</li> <li>Correlation length in z</li> </ul>	<ul> <li>Sand porosity</li> <li>Clay porosity</li> <li>Sand density</li> <li>Clay density</li> <li>van Genuchten m in sand</li> <li>van Genuchten m in clay</li> </ul>	<ul> <li>van Genuchten α in sand</li> <li>van Genuchten α in clay</li> <li>Permeability in sand</li> <li>Permeability in clay</li> <li>CO<sub>2</sub> diffusivity</li> <li>CO<sub>2</sub> leakage flux rate</li> </ul>

Source: Yunwei Sun's various presentations

## **Steps in uncertainty quantification (UQ)**

### Definition (of goals/objectives: what to do?)

simulation models, quantities of interest, assumptions

### Identification (sources of uncertainties: where?)

- model and data uncertainties
- Characterization (of uncertainty sources, what form?)
  - parametric distributions (priors) and/or model form
  - Aleatoric/epistemic, continuous/discrete
- Propagation (of uncertainty through models: how?)
  - forward and backward
- Analysis (of impact of uncertainties: so what?)
  - sensitivity analysis, risk analysis, ...

### of all relevant uncertainties in simulation models







# Simple uncertainty analysis may turn out to be computationally expensive

$$m(Y) = \int_{W} \underbrace{Y(W)}_{V} p(W) dW \quad \max_{\Omega} Y(\omega) - \min_{\Omega} Y(\omega)$$
variance
$$\int_{W} \underbrace{[Y(W)]^{2} p(W) dW - m^{2}(Y)}_{W}$$

+ higher order moments

- Y(ω) may be expensive to evaluate
- Sufficient accuracy may require many integration points
  - Highly nonlinear functions, may be nonsmooth
  - High dimensional uncertain parameter space
- Response surface (surrogate, emulator, ROM)
- Dimension reduction (parameter screening)

**Bayesian inference/Parameter Estimation/Calibration** 

## **Continuous Variables**

 $\pi(W|D) = p(D|W)p(W) / \hat{0} p(D|W)p(W)$ 

- Solution method: MCMC-like methods
  - for aleatoric uncertainties  $\rightarrow$  posterior distributions
  - for epistemic uncertainties →feasible subspace
- These methods are computationally very expensive
  - need large sample sizes for burn-in and generating posteriors
- In practice, these are calculated using response surfaces
- More complex cases: mixed continuous/discrete



## **Global Sensitivity Analysis**

#### First order sensitivity analysis

$$h_i^2 = \hat{0} \stackrel{\text{\acute{e}}}{=} \hat{0} \stackrel{\text{\acute{e}}}{=} \hat{0} Y(W_{\sim i} | W_i) p(W_{\sim i} | W_i) dW_{\sim i} - m(Y) \stackrel{\text{\acute{u}}}{=} p(W_i) dW_i / S^2$$

**Total order sensitivity indices** 

$$TS_{i} = \grave{0}\overset{\acute{e}}{\ddot{e}}\grave{0}\left(Y(W_{i} \mid W_{\sim i})p(W_{i} \mid W_{\sim i})dW_{i}\right)^{2} - m^{2}(Y(W_{\sim i}))\overset{\grave{u}}{\mu}p(W_{\sim i})dW_{\sim i}/S^{2}$$

- Variance-based SA is computationally expensive
  - need many integration points for accuracy
- In practice, these are calculated using response surfaces
  - the use of parametric forms reduce computational cost further

# In complex applications, these typical UQ analysis will be performed hierarchically





## **Major Themes in UQ Analysis Methods**

- Dimension reduction methods
  - High-dimensional physics parameter space (subset selection)
  - High-dimensional model output space (principal components)
- Response surface (surrogate, emulators) methods
  - Surrogate model selection (splines, GP, regression, ..)
  - Exploit smoothness in the approximate mapping
  - Response surface validation
- Basic uncertainty analysis
  - Statistical moments
  - Correlation analysis, ANOVA
- Calibration/Data integration
  - Bayesian-like inferences (filtering, gates, sets)
- Quantitative sensitivity analysis methods
  - Variance decomposition (1<sup>st</sup>, 2<sup>nd</sup>, group, and total order)
- Parameter study/design exploration
- Reliability analysis



#### How to make these UQ methods available to users?





### **PSUADE** is a software to facilitate UQ analysis



A Problem Solving Environment for Uncertainty Analysis and Design Exploration



## **A Simple UQ Workflow**



#### Lawrence Livermore National Laboratory

17 LLNL-PRES-XXXXXX

## **A Suite of Dimension Reduction Methods**

- Parametric methods (e.g. linearity/monotonicity assumptions)
  - derivative-based methods (local)
  - Standardized regression coefficient (SRC)
  - Spearman rank correlation coefficients (SRRC)
  - Plackett-Burman
  - Fractional factorial
  - Gradient-based Methods (global)
  - Morris method and its variants (e.g. modified Morris)
- Approximate emulator methods (global)
  - e.g. splines, Gaussian process, etc.
- Methods based on nearest neighbors (global)
  - Delta test, ...
- Tree-based methods (global)
  - Classification and regression tree (CART) + bootstrap

nonparametric methods are more suitable for multiphysics models



# A Suite of Response Surface Methods + Validation + Visualization



## **Adaptive Response Surface Analysis**



### **Example: a carbon capture absorber system**

Objective: quantify uncertainty in % of CO2 capture

#### Rate-based reactions

- 7 eqns: 3 equilibrium/4 kinetic
- Kinetic eqns: rate constant k<sub>n</sub> (A4-A7)

## Mass transfer

- Use the Hanley model
- UQ study restricted to tuning the interfacial area factor that affects the mass transfer rates (AE)



#### **Example:** a carbon capture absorber system



**RSA: training and test sets (~5000 each)** 

### **Example: CCSI UQ System Architecture**



## **Gasification simulations for Scale-up – with VVUQ**





## **Example: UQ Workflow for NRAP**



Source: Yunwei Sun's various presentations



## PSUADE download site:

## https://computation.llnl.gov/casc/uncertainty\_quantification



## THE END