



# Integration of High-Fidelity CO<sub>2</sub> Sorbent Models at the Process Scale Using Dynamic Discrepancy

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## Overview

#### Introduction: PEI adsorbents and reaction kinetics

Motivation and new mechanism

> Dynamic discrepancy reduced model and Bayesian calibration

Conclusions and future work





#### Introduction: Amine-based Adsorbents





SEM (a), TEM (b), HRTEM (c) images and particlesize distribution histogram (d) of the S600-10 sample



PEI structure





Length scale: (1) macroporosity (2) meso-porous particles (3) Silica-PEI composite

Mass transport:

Gas phase diffusion in mesopores;

Solid state diffusion in silica-PEI composites.

Yao, L., et al., Journal of colloid and interface science 408 (2013): 173-180 Mebane, D.S., et al., The Journal of Physical Chemistry C 117.50 (2013): 26617-26627.





# Introduction: Reaction Kinetics

• Zwitterion Mechanism

 $R_2NH + CO_2(g) \rightleftharpoons R_2NH^+CO_2^ R_2NH^+CO_2^- + B \rightleftharpoons R_2NCO_2^- + BH^+$ 

Termolecular Mechanism

 $R_2NH\cdots B + CO_2(g) \Longrightarrow R_2NCO_2^- + BH^+$ 





## Motivation





The effect of temperature on the CO<sub>2</sub> adsorption–desorption performance of KIT-6-PEI 50

Comparison of the adsorbed volume of CO2 from simulated dry and moist flue gas.

W.J. Son et al., Microporous and Mesoporous Materials 113 (2008) 31-40 Li, P., et al., Langmuir, 2008, 24 (13): 6567-6574







#### New Mechanism





# New Mechanism





#### New Mechanism

$$R_2 NH \cdots NHR_2 + CO_2(g) \rightleftharpoons^{\kappa_1} R_2 NH^+ CO_2^- - R_2 NH$$
 (1)

$$\mathbf{R}_{2}\mathbf{N}\mathbf{H}^{+}\mathbf{C}\mathbf{O}_{2}^{-}-\mathbf{R}_{2}\mathbf{N}\mathbf{H} \xrightarrow[k_{-2}]{k_{2}} \mathbf{R}_{2}\mathbf{N}\mathbf{C}\mathbf{O}_{2}^{-}:\mathbf{R}_{2}\mathbf{N}\mathbf{H}_{2}^{+}$$
(2)

$$R_2NH + H_2O(g) \rightleftharpoons^{\kappa_3} R_2NH - H_2O$$
 (3)

$$R_2 NH - H_2 O + CO_2(g) \stackrel{\kappa_4}{\longrightarrow} R_2 NH^+ CO_2^- - H_2 O \qquad (4)$$

$$R_2NH^+CO_2^- - H_2O \xrightarrow[k_{-5}]{k_{-5}} R_2NCOO^- : H_3O^+$$
 (5)

Variables:  $z_1 = \text{Amine-Zw}(1)$  x = Ammonium-Carbamate(2)

$$z_2 = Amine-H_2O(3)$$
  $z_3 = H_2O-Zw(4)$ 

y = Hydronium-Carbamate (5)

Solutions:



$$W_{CO_{2}} = M_{CO_{2}}n_{v}(x + y + z_{1} + z_{3})/\rho$$
  

$$W_{H_{2}O} = M_{H_{2}O}n_{v}(y + z_{2} + z_{3})/\rho$$
  
**Los Alamos**  
**NATIONAL LABORATORY**  
**EST. 1943**



## Simulation Results on Temperature Effect









# **Experiment and Simulation Results**









#### Methods: Bayesian Calibration and Dynamic Discrepancy

Bayesian Calibration:

 $egin{aligned} \mathcal{P}(A|B) &= rac{\mathcal{P}(B|A)\mathcal{P}(A)}{\int_{A'}\mathcal{P}(B|A')dA'} \ \mathcal{Z} &= Y( heta) + \delta(\xi) + \epsilon(\psi) \end{aligned}$ 

 $\Omega(\theta, \xi, \psi|Z) \propto \mathcal{L}(Z|\theta, \xi, \psi) \pi(\theta, \xi, \psi)$ 

Dynamic Discrepancy:

Discrepancy on Kinetic non-ideality :

Discrepancy on Thermodynamic Equilibrium

$$u_{b_{i}}^{*} = \zeta_{b} \exp\left(\frac{-\Delta H_{b}^{\ddagger}}{RT}\right)$$
$$u_{b_{i,new}}^{*} = \zeta_{b} \exp\left(\frac{-\Delta H_{b}^{\ddagger}}{RT}\right) \exp[\delta(z_{i-1}, z_{i}, z_{i+1}, \frac{1}{T})]/T$$
$$= u_{b_{i}}^{*} \exp[\delta(z_{i-1}, z_{i}, z_{i+1}, \frac{1}{T})]$$

$$\kappa = \exp{\left(\frac{-\Delta H + T\Delta S}{RT}\right)} / P$$

$$\kappa_{new} = \kappa * \exp[\delta^{E}(P, T)]$$





# Reduced Model







# **Calibration Results**







### Calibration Results









# Conclusion



- A new mechanism using amine and water stabilized zwitterions as diffusive intermediates has been proposed
- Model simulation replicated the experiment results qualitatively
- Bayesian calibration and dynamic discrepancy implemented in the model to get quantitatively matched results
- Reduced model is used to improve the calculation speed

# Future Work

- Apply this model to bubbling fluidized bed model
- Quantify the uncertainty from model reduction and model upscaling







## Upscaling Results



Bhat, K.S., et al., arXiv preprint arXiv:1411.2578 (2014).







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