

Process Systems Engineering

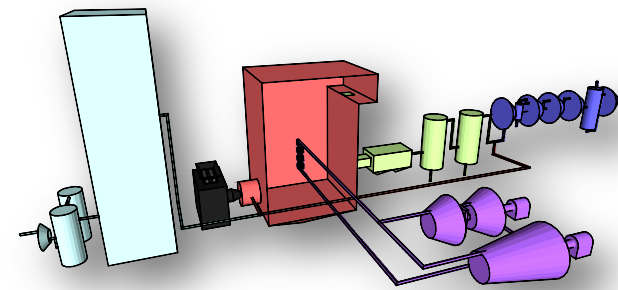
Equation Oriented Coal Oxycombustion Flowsheet Optimization

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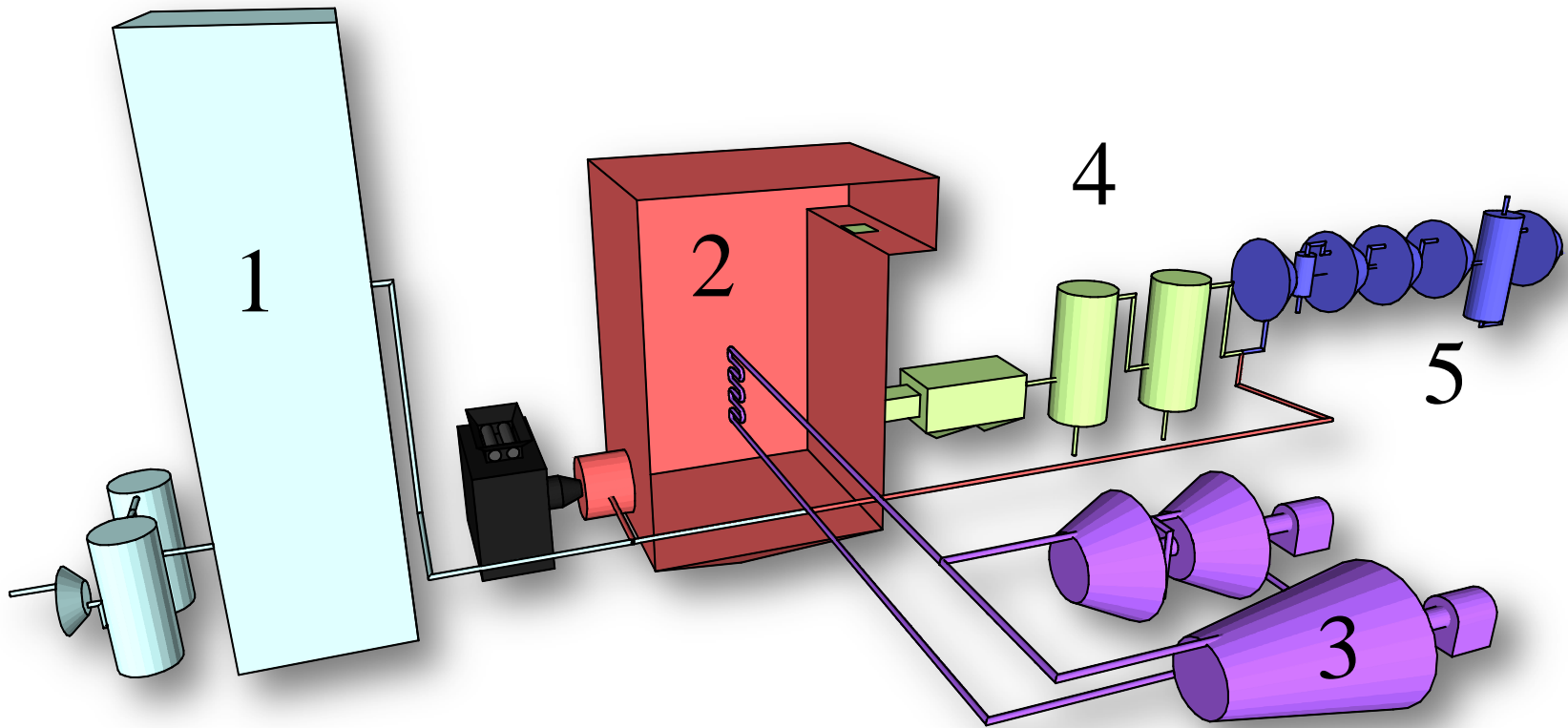
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Oxycombustion Flowsheet



1. Air Separation Unit
2. Boiler
3. Steam Turbine

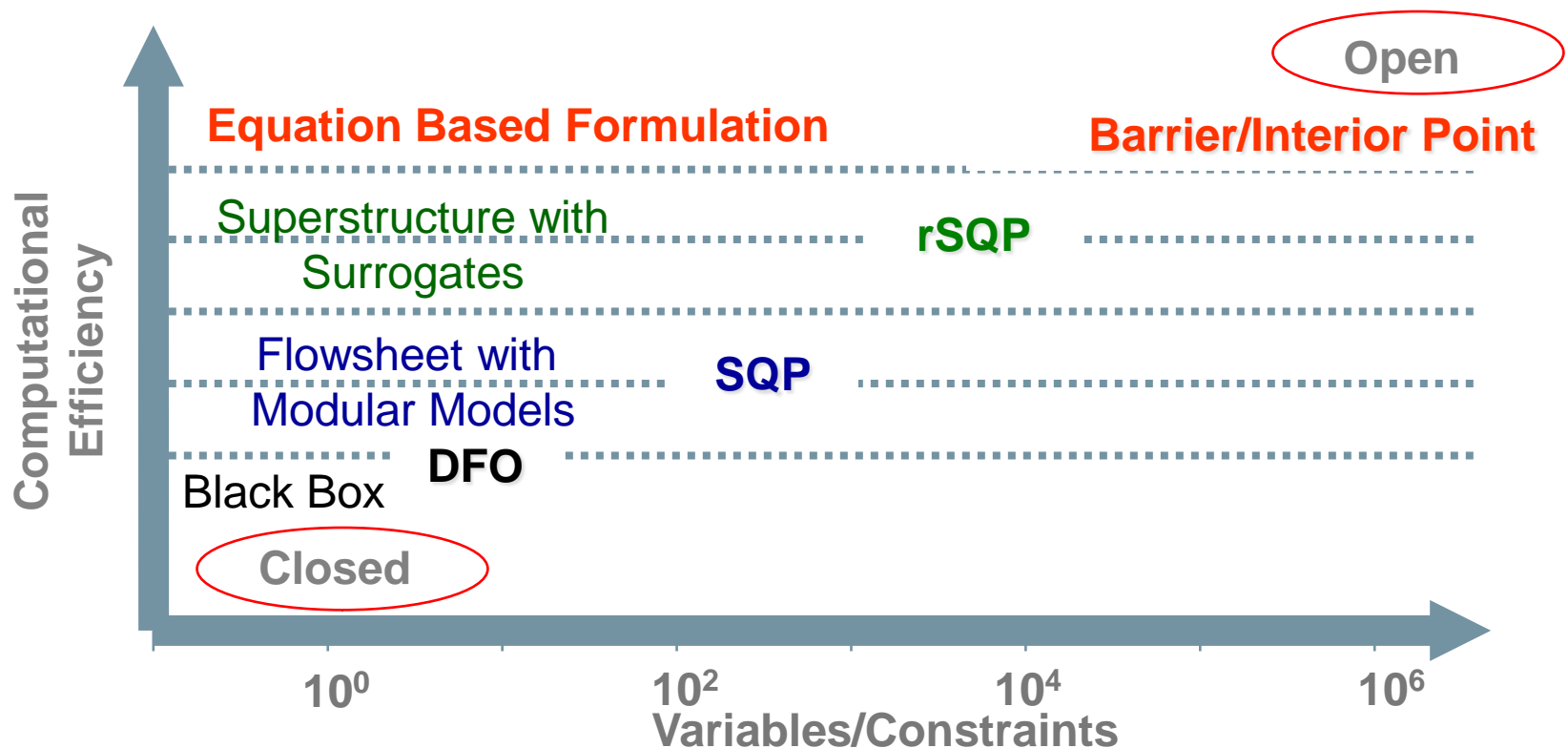
4. Pollution Controls
5. CO₂ Compression Train

Project Objective

Tightly coupled
subsystems

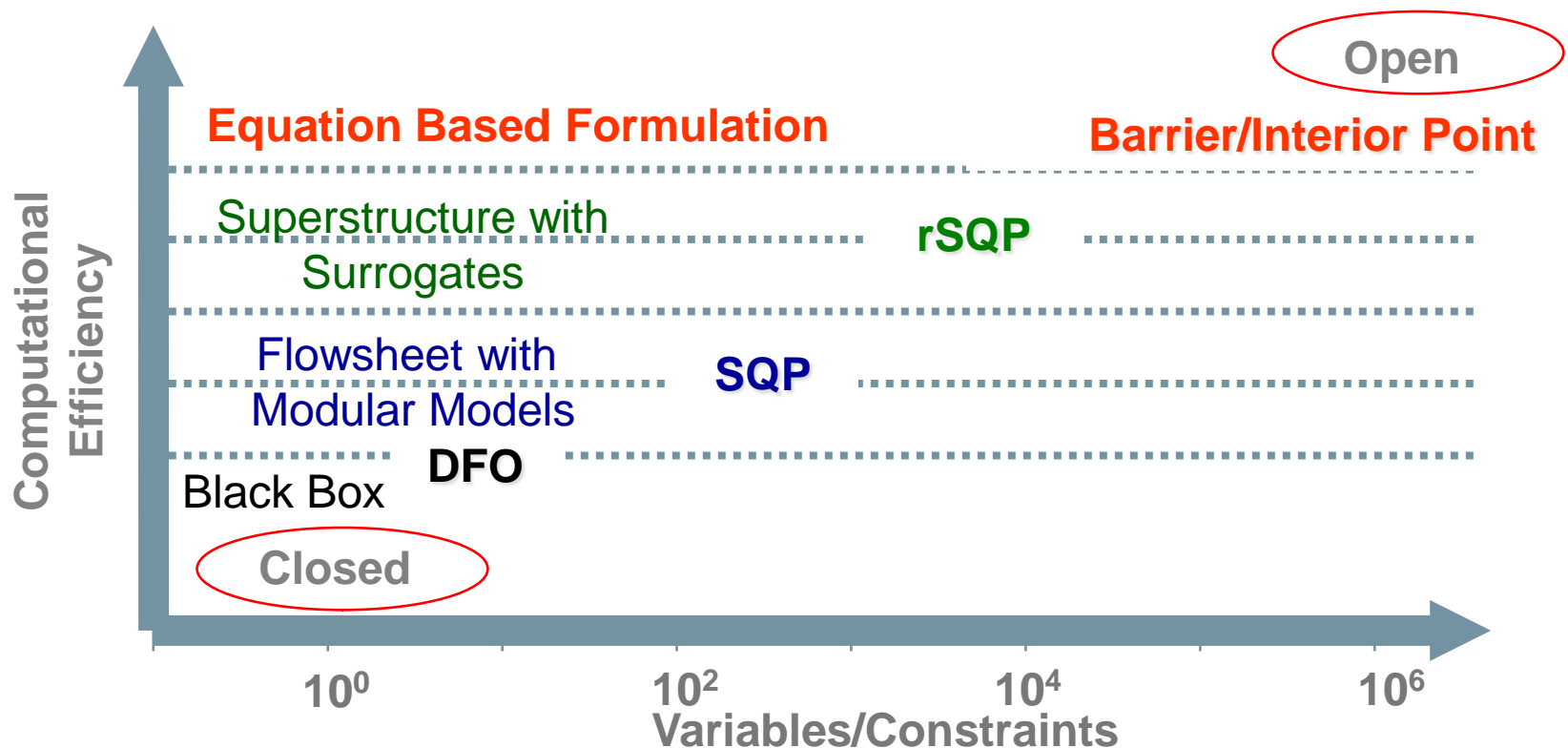


Optimize using
detailed models



Project Objective

Develop an **equation oriented** framework to optimize an entire coal oxycombustion flowsheet.

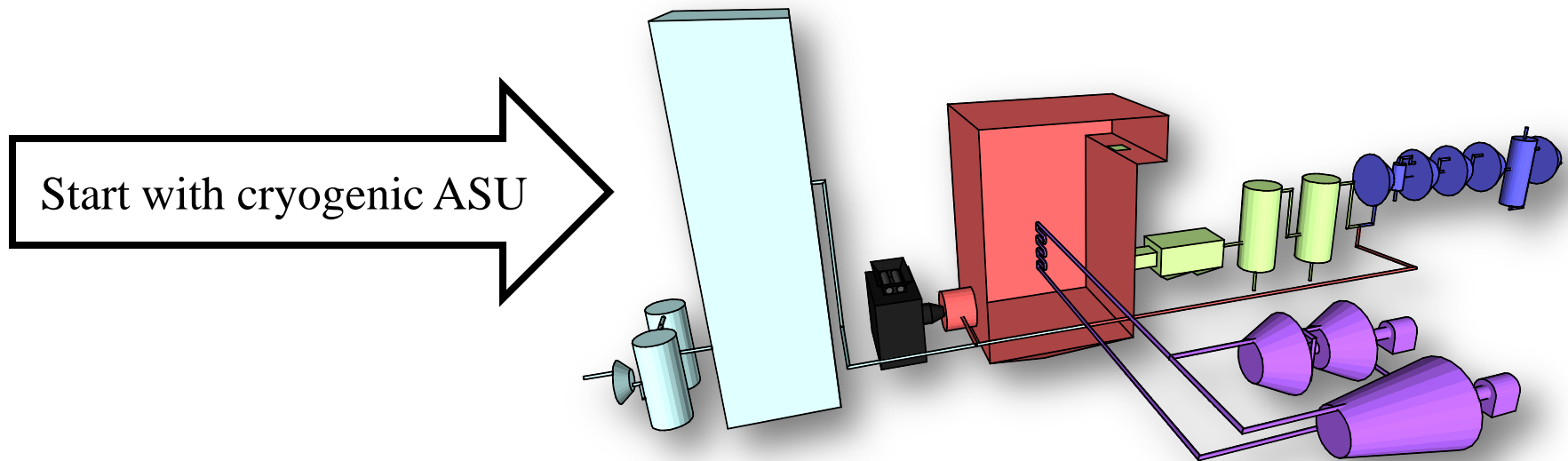


Project Objective

Goal: Consider complex trade-offs in flowsheet.

What is the optimal flue gas recycle ratio?

Are there heat integration synergies with the ASU & CPU?



Cryogenic Air Separation

Boiling Points @ 1 atm

Oxygen: -183 °C

Argon: -185.7 °C

Nitrogen: -195.8 °C

Multicomponent
distillation with tight heat
integration

Low pressure
section

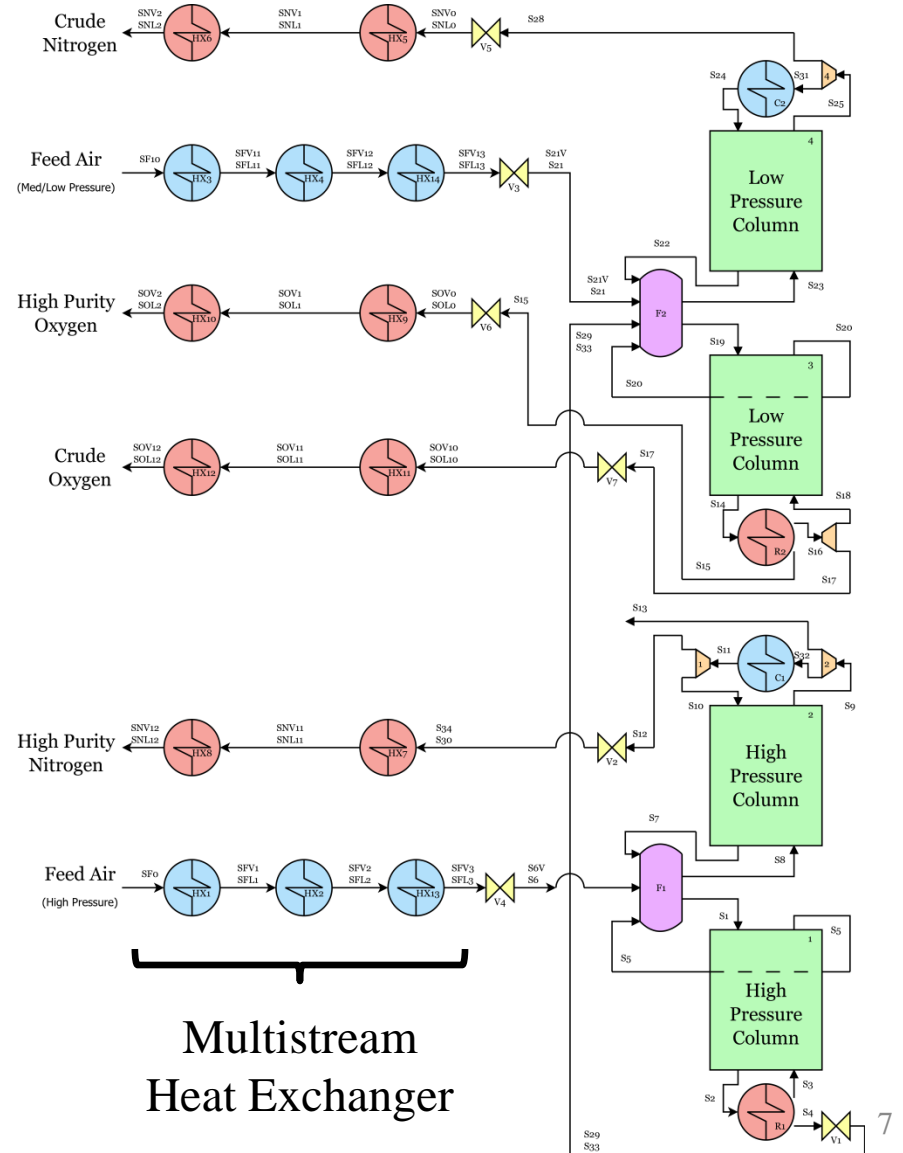
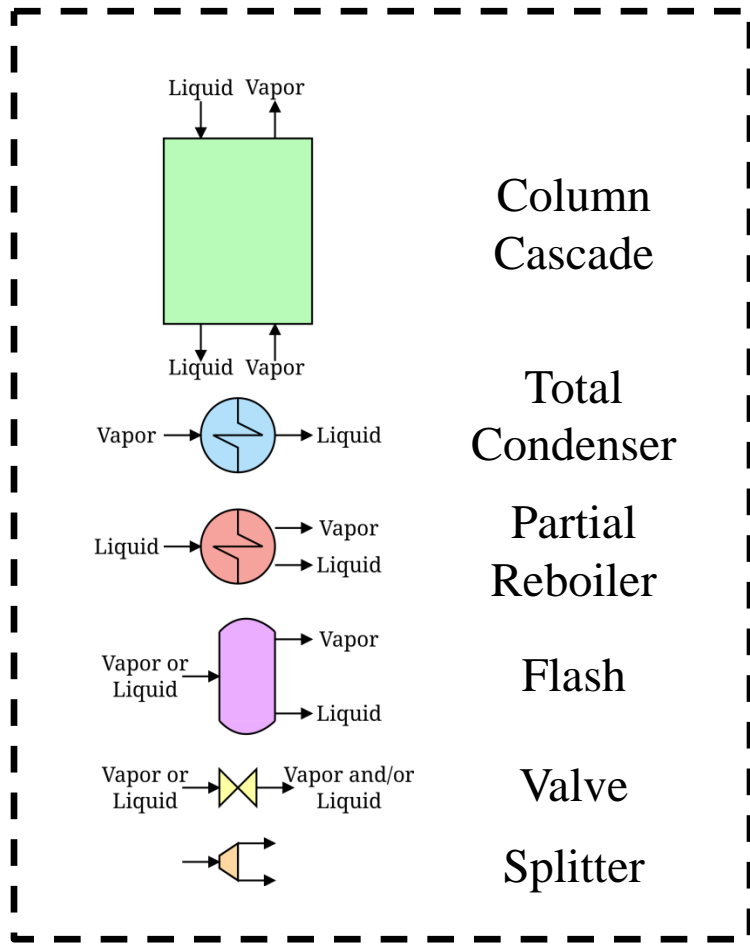


Photo from wikipedia.org

High pressure
section

Challenging to systematically optimize in AspenPlus.

Double Column Configuration



ASU: Optimization Formulation

min ASU Compression Energy
(kWh / kg O₂ product)

s.t.  Thermodynamics Module 

Unit Operation Models

 Cascade Model 

Flowsheet Connectivity

 Heat Integration 

O₂ product purity \geq 90 mol%

Note: **Upper and lower bounds not shown above** where considered for many variables including stream/equipment temperatures and pressures.

Cubic Equations of State

$$f(Z_s) = Z_s^3 - Z_s^2 + (A_s - B_s - B_s^2)Z_s - A_sB_s = 0$$



Examples: Peng-Robinson, Soave-Redlich-Kwong

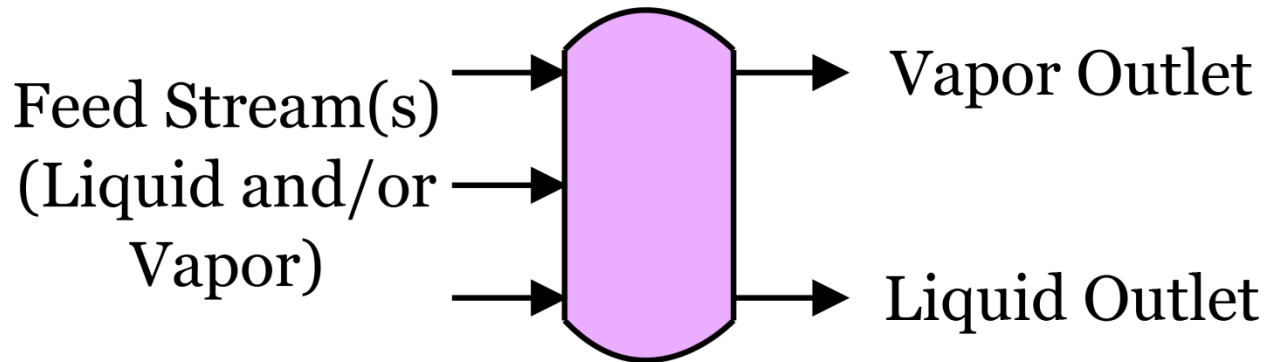
Phase	CEOS	1 st Derivative	2 nd Derivative
Liquid	$f(Z_s) = 0$	$f'(Z_s) \geq 0$	$f''(Z_s) \leq 0$
Vapor	$f(Z_s) = 0$	$f'(Z_s) \geq 0$	$f''(Z_s) \geq 0$

$$f'(Z_s) = 3(Z_s)^2 - 2Z_s + (A_s - B_s - (B_s)^2) \geq 0$$

$$f''(Z_s) = 6Z_s - 2 \geq 0, \quad s \in \{\text{Vapor Streams}\}$$

$$f''(Z_s) = 6Z_s - 2 \leq 0, \quad s \in \{\text{Liquid Streams}\}$$

Flash Example & Thermodynamics



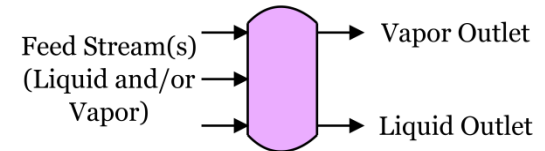
Material Balance
$$\sum F_c^{in} = F_c^v + F_c^l$$

Energy Balance
$$\sum F^{in} H^{in} = F^v H^v + F^l H^l$$

Phase Equilibrium
$$y_c^v = K_c x_c^l$$
$$K_c = \frac{\phi_c^l}{\phi_c^v}$$

Phase Disappearance

Thermodynamics must be relaxed
when a phase disappears.



Thermodynamics Relaxation

$$f''(Z^l) \leq M \sigma^l$$

$$f''(Z^v) \geq -M \sigma^v$$

Complementarity Condition

$$0 \leq F^v \perp \sigma^v \geq 0$$

$$0 \leq F^l \perp \sigma^l \geq 0$$

Phase Equilibrium

$$y_c^v = \beta K_c x_c^l$$

$$K_c = \frac{\phi_c^l}{\phi_c^v}$$

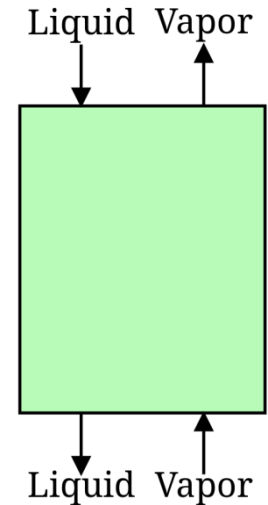
Equilibrium Relaxation

$$-\sigma^l \leq \beta - 1$$

$$\beta - 1 \leq \sigma^v$$

Cascade Model

- Group method
 - Continuous number of ideal stages
 - Based on work of Kremser and Edmister
 - Requires specification of stripping and absorbing section
- Modifications for distillation:
 - Exit streams at dew/bubble point
 - Decrease vapor at bottom = increase liquid at top



Kamath, Grossmann & Biegler (2010). Aggregate models based on improved group methods for simulation and optimization of distillation systems. *Computers & Chemical Engineering*.

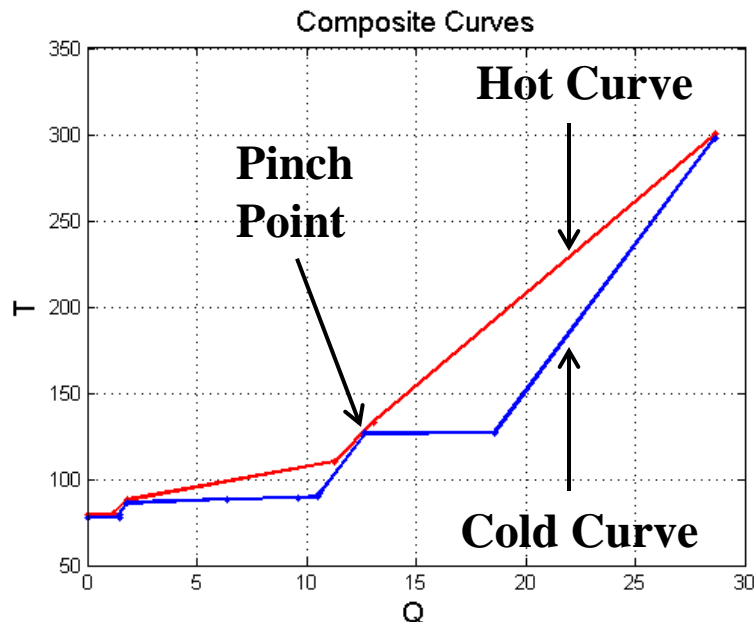
ASU: Heat Integration Model

Pinch candidates

Based on work of Duran & Grossmann (1986)

Available heating and cooling above pinch

Utility calculations



$$T^p = \begin{cases} T_p^{in} & \text{if candidate } p \text{ is a hot stream} \\ T_p^{in} + \Delta T_{min} & \text{if candidate } p \text{ is a cold stream} \end{cases}$$

$$QA_H^p = \sum_{i \in \{Hot\}} FCp_i [\tilde{\max}(T_i^{in} - T^p) - \tilde{\max}(T_i^{out} - T^p)]$$

$$QA_C^p = \sum_{j \in \{Cold\}} FCp_j [\tilde{\max}(T_j^{out} - T^p + \Delta T_{min}) - \tilde{\max}(T_j^{in} - T^p + \Delta T_{min})]$$

$$Q_s \geq QA_C^p - QA_H^p \quad \text{for all } p$$

$$Q_w = Q_s + \sum_{j \in \{Cold\}} Q_j^{in} - \sum_{i \in \{Hot\}} Q_i^{out}$$

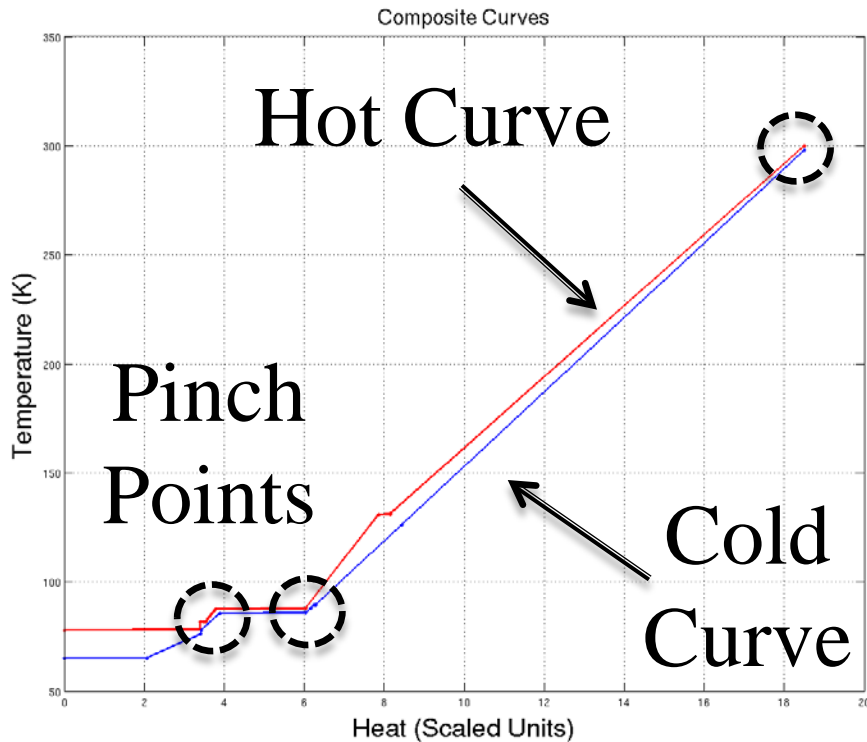
Implementation Details

- Medium-size non-convex problem
 - 4418 variables
 - 4586 constraints
- Automated initialization procedure
- Solved using **CONOPT3** in GAMS (General Algebraic Modeling System)
 - **3 minutes** with an Intel i7 processor

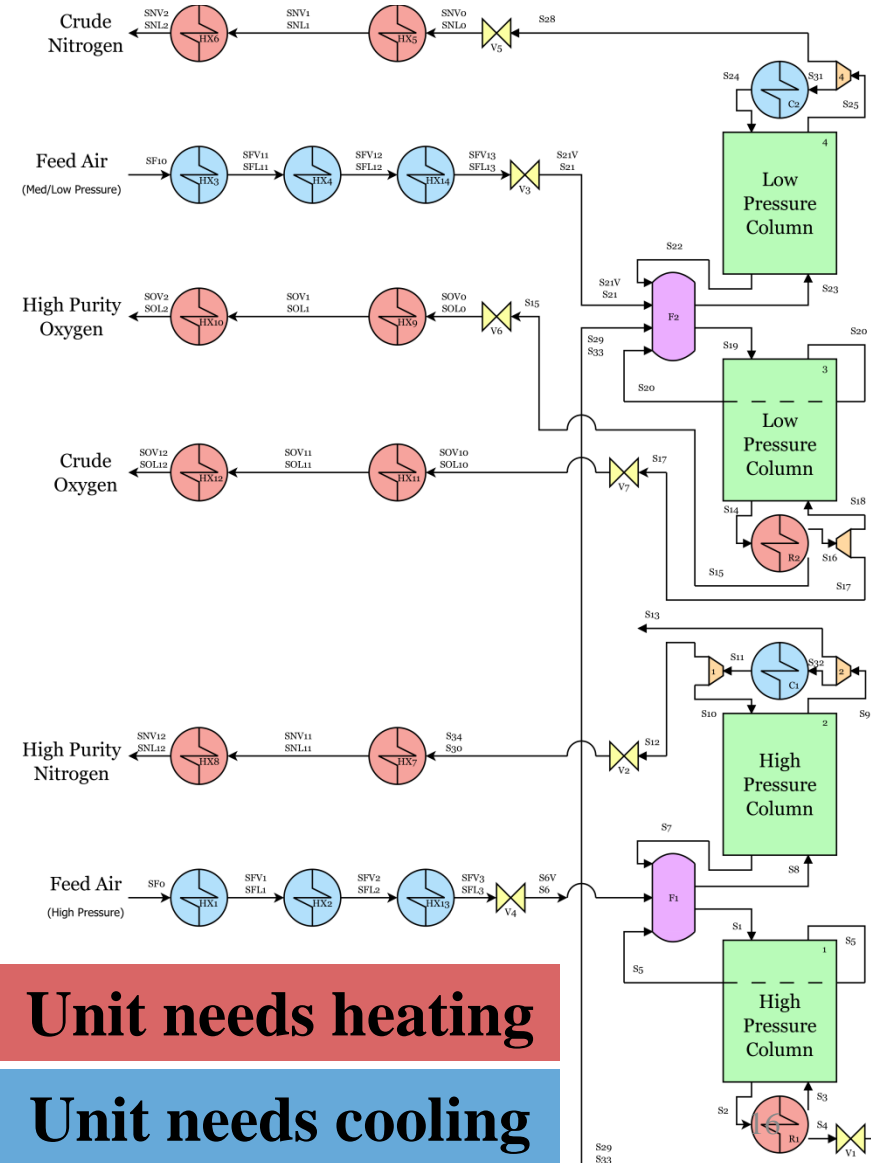
Results Summary for 90 mol% O₂

- Energy usage: **0.17 kWh/kg O₂**
typical designs: **~0.22 kWh/kg O₂**
- Low pressure column (LPC): **19 stages**
High pressure column (HPC): **11 stages**
- LPC: **1.0 bar** literature: **1.7 – 4.3 atm**
HPC: **2.5 bar** literature: **6.8 – 13.5 atm**
- Only $\frac{1}{4}$ of feed air sent to HPC
typical designs: **all**

Heat Integration Results

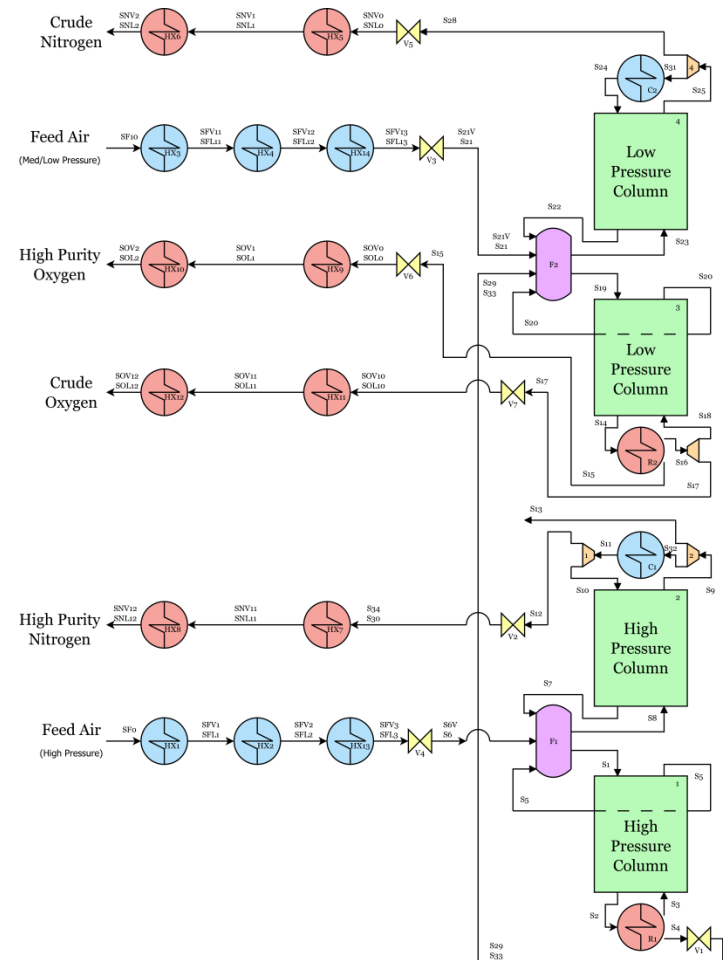


No external cooling or heating required



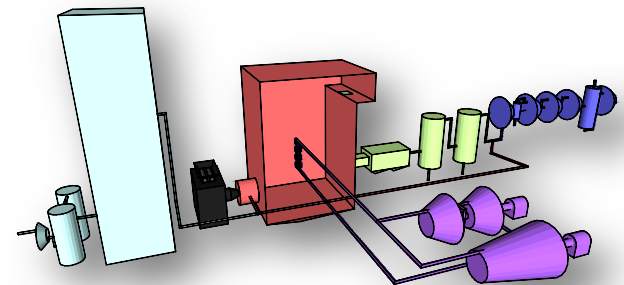
Future ASU Work

- Explore alternate ASU configurations and applications
 - Elevated pressure ASU?
 - Side draws?
- Model capital costs and re-optimize



Future Flowsheet Work

- Integrate ASU model with remaining flowsheet sections
- Explore potential heat integration synergies
 - ASU with post combustion cryogenics
 - ASU with compression train
 - Compression train with boiler
 - Feed water heater train design

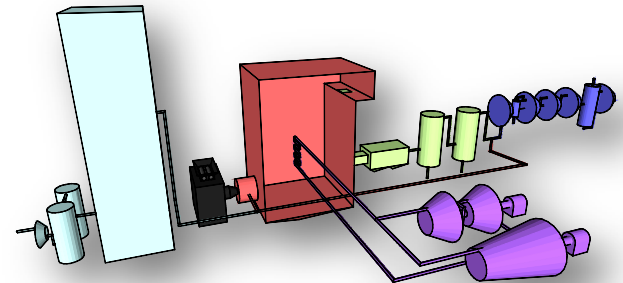


Conclusions

Optimized ASU with equation-based model:

- Cubic equation of state with accurate derivatives
- Pinch location heat integration
- Pure nonlinear program – no discrete variables

Acknowledgements:



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